

## The Vibrational Spectra of Water of Crystallization in Barium Chlorate Monohydrate, Calcium Sulfate Dihydrate and Copper Chloride Dihydrate Crystals

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Infrared spectra of water of crystallization and heavy water of crystallization were measured for  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ ,  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ ,  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ ,  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{D}_2\text{O}$ ,  $\text{CaSO}_4 \cdot 2\text{D}_2\text{O}$ , and  $\text{CuCl}_2 \cdot 2\text{D}_2\text{O}$ , in which the divalent metal ion lies on the bisector line of H—O—H angle or D—O—D angle. From a comparison of the spectra, assignment of the infrared absorption bands was made for the rotational and the translational vibrations of the water of crystallization.

Water of crystallization is classified into several types by the mode of bonding with surrounding atoms and ions.<sup>1)</sup> It was reported<sup>2-4)</sup> that the optically active lattice vibration frequencies associated with water of crystallization change sensitively with the change of its state of bonding. In the present study, barium chlorate monohydrate,  $\text{Ba}(\text{ClO}_3)_2 \cdot 2\text{H}_2\text{O}$ , calcium sulfate dihydrate,  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ , copper chloride dihydrate,  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  (type D in Chidambaram's classification<sup>1)</sup>) were chosen as representatives of the crystals in which water of crystallization coordinates with a divalent metal ion on the bisector line of H—O—H angle,<sup>5-7)</sup> and their bands due to water of crystallization were measured and assigned on the basis of the spectral change on deuteration.

### Experimental

The samples were obtained by recrystallization of  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$  of guaranteed grade, Kanto Chemical Co., Inc.,  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  of guaranteed grade, Wako Pure Chemical Industries Ltd., and  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  of guaranteed grade,

Kanto Chemical Co., Inc. from their aqueous solutions. The deuterates of  $\text{Ba}(\text{ClO}_3)_2 \cdot 2\text{H}_2\text{O}$  and  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  were prepared as residues obtained by vacuum distillation of their heavy water solutions. The deuterate of  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  was obtained by exposure of  $\text{CuCl}_2$  to  $\text{D}_2\text{O}$  vapor overnight in a small sealed bottle.

IR spectra in the region  $4000\text{--}400\text{ cm}^{-1}$  were measured with the Nujol mulls of  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ ,  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ , and their deuterates, and those of  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  and its deuterate with the Nujol mulls placed between KBr plates covered with thin polyethylene sheets to avoid reaction of the samples with KBr plates. Far IR spectra ( $400\text{--}30\text{ cm}^{-1}$ ) of  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ ,  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  and their deuterates were measured with their Nujol mulls placed between two polyethylene plates of 2 mm thickness, while those of  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$  and its deuterate were measured with a solid paraffin-sample mixture prepared by dispersing the sample powder into molten paraffin and solidifying the mixture cast on a polyethylene plate. The spectra are shown in Figs. 1—6.

Infrared spectra of  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  above  $300\text{ cm}^{-1}$  have been reported by many investigators.<sup>8-10)</sup> The spectra of  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  above  $300\text{ cm}^{-1}$  in Figs. 3 and 4 are given mainly for the sake of comparison with those of its deuterate. A Hitachi EPI-G3 Infrared Spectrophotometer and a FIS-3 Far Infrared Spectrometer were used.

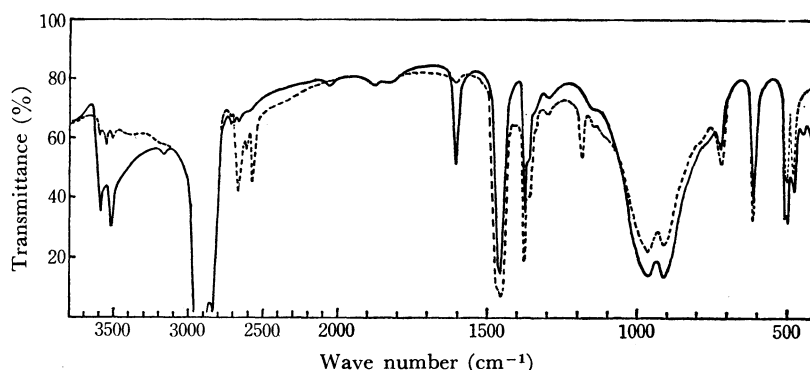


Fig. 1. Infrared spectra of barium chlorate monohydrate in Nujol mull (solid line) and its deuterate in Nujol mull (broken line).

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### Discussion

The relative intensities of O—H stretching and H—O—H bending bands are much weaker than those

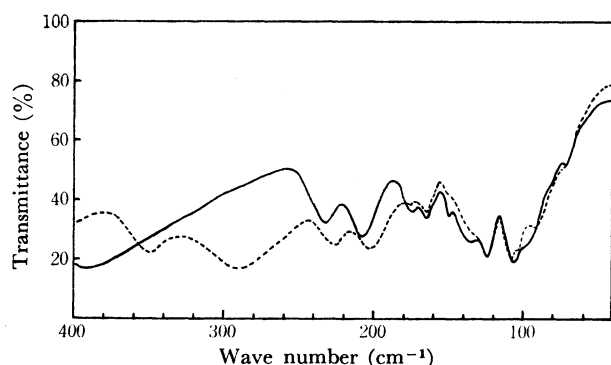


Fig. 2. Far infrared spectra of barium chlorate monohydrate dispersed into solid paraffin (solid line) and its deuterate dispersed into solid paraffin (broken line).

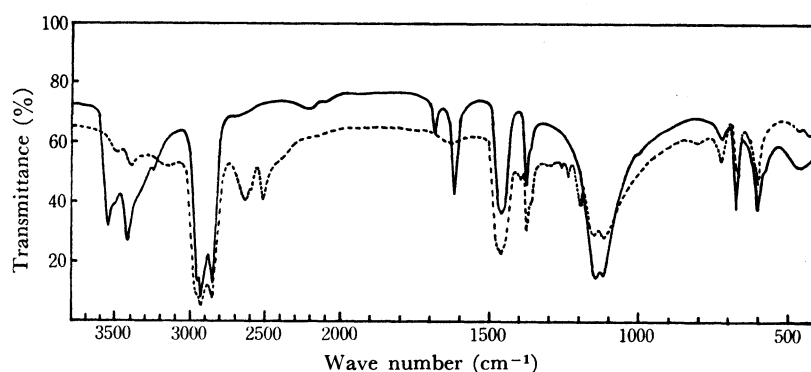


Fig. 3. Infrared spectra of calcium sulfate dihydrate in Nujol mull (solid line) and its deuterate in Nujol mull (broken line).

TABLE 1. FREQUENCIES IN  $\text{cm}^{-1}$  OF IR BANDS OF WATER OF CRYSTALLIZATION

$\text{Ba}(\text{ClO}_3)_2 \cdot \text{H}_2\text{O}$ $\nu_{\text{H}}$	$\text{Ba}(\text{ClO}_3)_2 \cdot \text{D}_2\text{O}$ $\nu_{\text{D}}$	$\nu_{\text{H}}/\nu_{\text{D}}$	$\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$ $\nu_{\text{H}}$	$\text{CaSO}_4 \cdot 2\text{D}_2\text{O}$ $\nu_{\text{D}}$	$\nu_{\text{H}}/\nu_{\text{D}}$	$\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$ $\nu_{\text{H}}$	$\text{CuCl}_2 \cdot 2\text{D}_2\text{O}$ $\nu_{\text{D}}$	$\nu_{\text{H}}/\nu_{\text{D}}$
451	350	1.29	576	432	1.33	*	360	
390	290	1.34	460	345	1.33	430	315	1.36
*	*		306	259	1.18	310	255	1.22
			271	212	1.28	243	223	1.09
233	226	1.03						
207	203	1.02						

\* Not observed because of weak intensity and overlapping with other bands.

TABLE 2. CALCULATED MOMENTS OF INERTIA OF  $\text{H}_2\text{O}$  AND  $\text{D}_2\text{O}$  MOLECULES IN  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  AND  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  AND THEIR DEUTERATES<sup>a)</sup> (IN  $10^{-40} \text{ g} \cdot \text{cm}^2$ )

	$I_{\text{A}}$	$I_{\text{B}}$	$I_{\text{C}}$	$\sqrt{I_{\text{A}, \text{D}_2\text{O}}/I_{\text{A}, \text{H}_2\text{O}}}$	$\sqrt{I_{\text{B}, \text{D}_2\text{O}}/I_{\text{B}, \text{H}_2\text{O}}}$	$\sqrt{I_{\text{C}, \text{D}_2\text{O}}/I_{\text{C}, \text{H}_2\text{O}}}$
$\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$	1.067	2.089	3.157			
$\text{CaSO}_4 \cdot 2\text{D}_2\text{O}$	1.919	4.174	6.093	1.34	1.41	1.39
$\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$	0.922	1.970	2.892			
$\text{CuCl}_2 \cdot 2\text{D}_2\text{O}$	1.658	3.936	5.594	1.34	1.41	1.39

a) The moments of inertia in the table were calculated using the bond length and bond angle of water of crystallization.<sup>5,9)</sup> The same bond length and bond angle as  $\text{H}_2\text{O}$  molecule in the crystals were assumed for  $\text{D}_2\text{O}$  molecule in the deuterate crystals.

of O—D stretching and D—O—D bending bands as shown in Figs. 1, 3, and 5. This indicates that the major component of each deuterate is  $\text{Ba}(\text{ClO}_3)_2 \cdot \text{D}_2\text{O}$ ,  $\text{CaSO}_4 \cdot 2\text{D}_2\text{O}$ , or  $\text{CuCl}_2 \cdot 2\text{D}_2\text{O}$ .

As shown in Fig. 6, the band of deuterated copper chloride dihydrate at  $223 \text{ cm}^{-1}$  corresponds to that of  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  at  $243 \text{ cm}^{-1}$ . The asymmetrical band of  $\text{CuCl}_2 \cdot 2\text{H}_2\text{O}$  at  $298 \text{ cm}^{-1}$  is interpreted to be composed of two overlapped bands at about  $310 \text{ cm}^{-1}$  and at  $298 \text{ cm}^{-1}$  from the fact that two bands appear at  $295 \text{ cm}^{-1}$  and  $255 \text{ cm}^{-1}$  for the deuterate and from a comparison of  $310/255$  value with the  $\nu_{\text{H}}/\nu_{\text{D}}$  values in Table 2. Similarly, the band of  $\text{CaSO}_4 \cdot 2\text{H}_2\text{O}$  at  $306 \text{ cm}^{-1}$  corresponds to that of the deuterate at  $259 \text{ cm}^{-1}$ .

Comparing the spectra of the crystals with those of their deuterates, a correspondence can be set up between the observed frequencies of the former and of the latter as shown in Table 1. For  $\text{Ba}(\text{ClO}_3)_2 \cdot 2\text{H}_2\text{O}$ ,

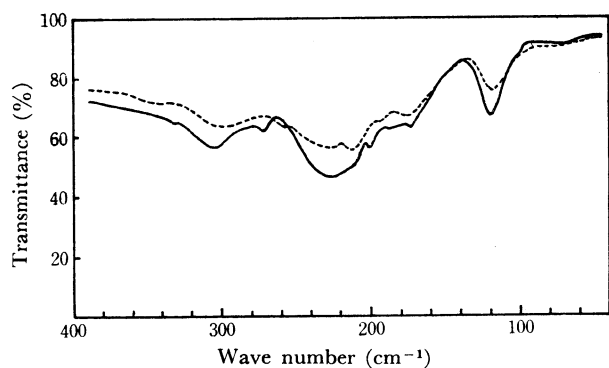


Fig. 4. Far infrared spectra of calcium sulfate dihydrate in Nujol mull (solid line) and its deuterate in Nujol mull (broken line).

Prask and Boutin observed<sup>11)</sup> neutron scattering peak frequencies of 458 cm<sup>-1</sup>, 390 cm<sup>-1</sup>, 318 cm<sup>-1</sup>, 238 cm<sup>-1</sup>, 212 cm<sup>-1</sup>, 149 cm<sup>-1</sup>, 81 cm<sup>-1</sup>, and 67 cm<sup>-1</sup> as those due to water of crystallization. The observed IR band frequencies, which were found to shift on deuteration, correspond to the frequencies observed by Prask and Boutin except for the frequencies 318 cm<sup>-1</sup>, 81 cm<sup>-1</sup>, and 67 cm<sup>-1</sup>. As shown in Table 1, the  $\nu_H/\nu_D$  values of 1.29 and 1.34 for the bands at 451 cm<sup>-1</sup> and 390 cm<sup>-1</sup>, respectively, lead to an assignment of the bands to the rotational vibrations of crystallization, while those of 1.03 and 1.02 for the bands at 233 cm<sup>-1</sup> and 207 cm<sup>-1</sup>, respectively, lead to an assignment of the bands to the translational vibrations of water of crystallization.

In the case of CaSO<sub>4</sub>·2H<sub>2</sub>O and CuCl<sub>2</sub>·2H<sub>2</sub>O, the

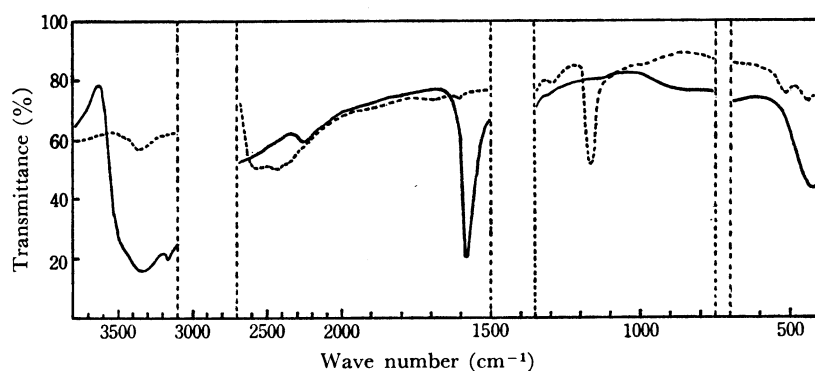


Fig. 5. Infrared spectra of copper chloride dihydrate in Nujol mull (solid line) and its deuterate in Nujol mull (broken line).

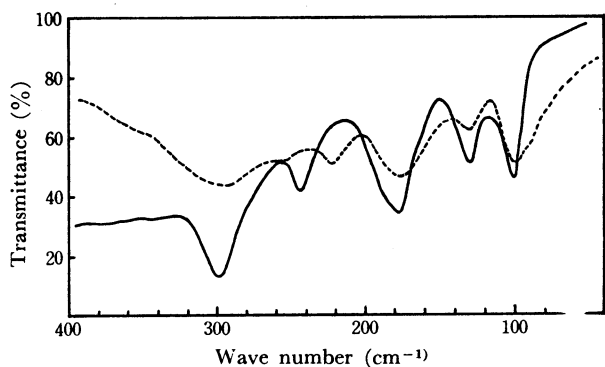


Fig. 6. Far infrared spectra of copper chloride dihydrate in Nujol mull (solid line) and its deuterate in Nujol mull (broken line).

bands at 576 cm<sup>-1</sup>, 460 cm<sup>-1</sup>, and 430 cm<sup>-1</sup>, are assigned to the rotational vibrations of water of crystallization on the basis of  $\nu_H/\nu_D$  values of 1.33, 1.33, and 1.36, respectively. The values are in accordance with the calculated values of  $\sqrt{I_{A,D_2O}/I_{A,H_2O}}$  and  $\sqrt{I_{C,D_2O}/I_{C,H_2O}}$  in Table 2. It is expected that  $\nu_H/\nu_D$  values of the translational vibrations of water of crystallization in CaSO<sub>4</sub>·2H<sub>2</sub>O and CuCl<sub>2</sub>·2H<sub>2</sub>O crystals differ from those of Ba(ClO<sub>3</sub>)<sub>2</sub>·H<sub>2</sub>O crystal since the reduced masses of Ca<sup>2+</sup>...OH<sub>2</sub> and Cu<sup>2+</sup>...OH<sub>2</sub> systems

differ from the mass of Ba<sup>2+</sup>...OH<sub>2</sub> system which is close to that of H<sub>2</sub>O molecule. Thus, the bands at 271 cm<sup>-1</sup> and 243 cm<sup>-1</sup>, which have different  $\nu_H/\nu_D$  values higher than those of the bands at 233 cm<sup>-1</sup> and 207 cm<sup>-1</sup> of Ba(ClO<sub>3</sub>)<sub>2</sub>·H<sub>2</sub>O can be assigned to the translational vibrations of water of crystallization. The bands at 306 cm<sup>-1</sup> and 310 cm<sup>-1</sup> have very close  $\nu_H/\nu_D$  values. This indicates that these bands can be assigned to the rotational rather than the translational vibrations.

It has been reported that the spectra of the rotational vibrations of water of crystallization change remarkably with the change of bound state of water of crystallization.<sup>2-4)</sup> Our results show that the spectra of water of crystallization having a coordinated divalent metal ion on the bisector line of H-O-H angle has a characteristic pattern, that is, the spectra consist of a broad band with medium intensity having two weaker bands on both sides, the characteristic spectra showing the difference corresponding to the different bound states of water of crystallization in the crystals. Interatomic distances in the crystals differ with the crystals. (Ba(ClO<sub>3</sub>)<sub>2</sub>·H<sub>2</sub>O, O<sub>w</sub>...Ba<sup>2+</sup> 2.60 Å, H<sub>w</sub>...O(ClO<sub>3</sub>) 2.77 Å; CuCl<sub>2</sub>·2H<sub>2</sub>O, O<sub>w</sub>...Cu<sup>2+</sup> 1.925 Å, H<sub>w</sub>...Cl- 2.258 Å; CaSO<sub>4</sub>·2H<sub>2</sub>O, O<sub>w</sub>...Ca<sup>2+</sup> 2.34 Å and 2.35 Å, H<sub>w</sub>...O(SO<sub>4</sub><sup>2-</sup>) 2.816 Å and 2.824 Å). These distances suggest that the water of crystallization of CuCl<sub>2</sub>·2H<sub>2</sub>O and CaSO<sub>4</sub>·2H<sub>2</sub>O is more strongly bound than that of Ba(ClO<sub>3</sub>)<sub>2</sub>·H<sub>2</sub>O. This seems to cause the shift of frequencies of the weak band and the broad band having higher frequencies than the other weak band.

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